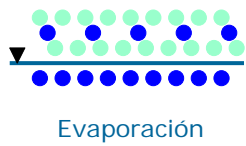
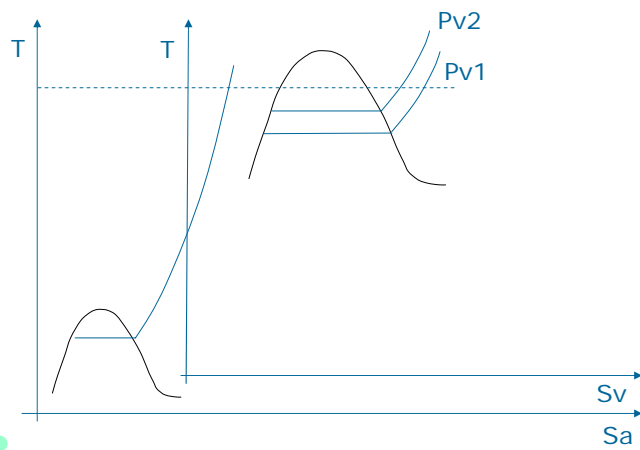
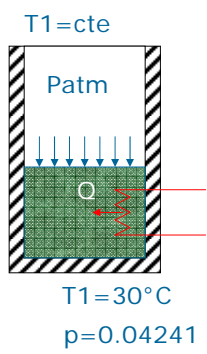
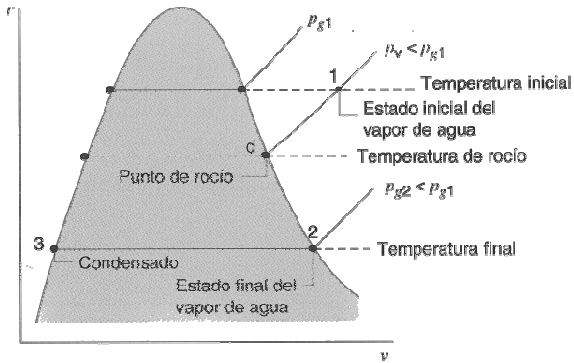




Aire húmedo



Temperatura de rocío

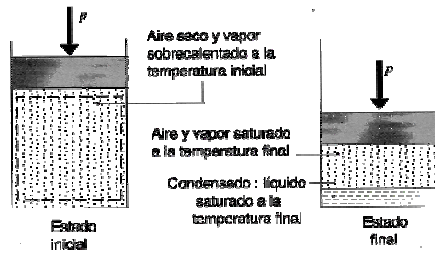


Enfriamiento a p=cte

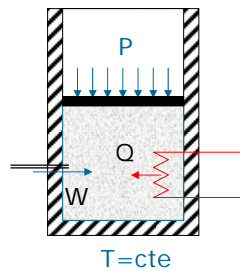
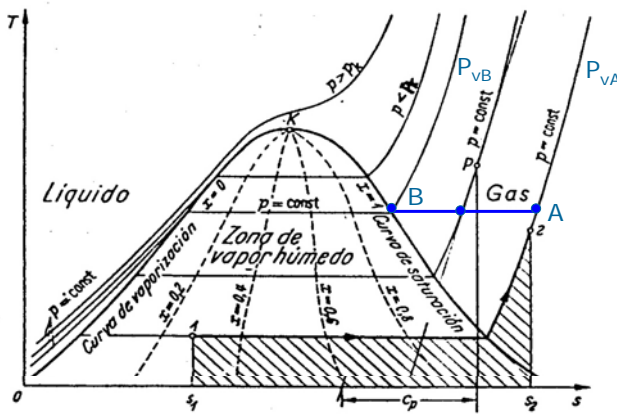
$$p_a = \frac{n_a}{n_a + n_v} \cdot p$$

$$p_v = \frac{n_v}{n_a + n_v} \cdot p$$

$$p = p_v + p_a$$



Humedad relativa



$$\frac{p_{vA}}{p_{vB}} = \frac{p_{v,t}}{p_{s,t}} \quad \psi = \frac{p_{v,t}}{p_{s,t}}$$

Humedad absoluta

Es la relación entre la masa de agua y la masa de aire seco

$$x = \frac{m_w}{m_a} \quad x = \frac{\cancel{m_w}}{m_a + \cancel{m_w}}$$

$$x = 0.622 \cdot \frac{p_v}{p - p_v}$$

$$x = \frac{M_w}{M_a} \cdot \frac{n_w}{n_a}$$

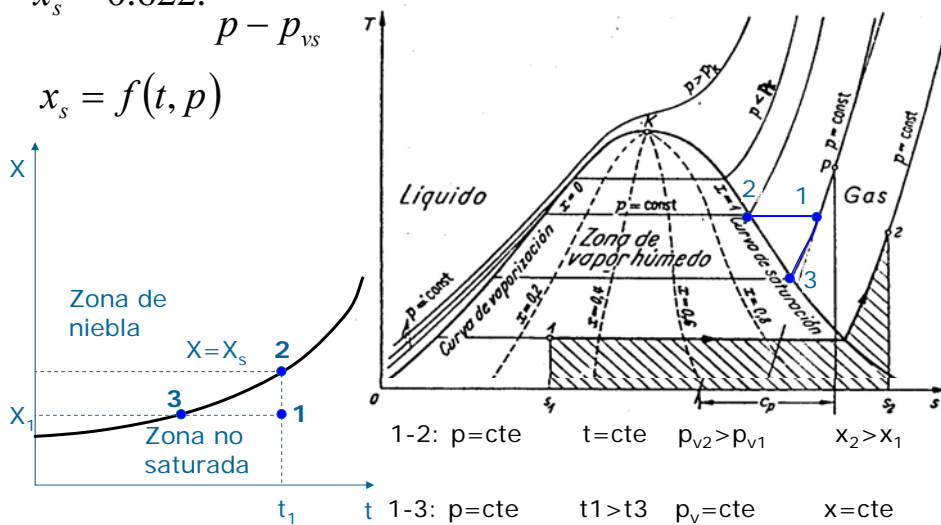
$$x = \frac{18.02}{28.97} \cdot \frac{n_w}{n_a} = 0.622 \cdot \frac{n_w}{n_a}$$

$$x = 0.622 \cdot \frac{p_v}{p_a}$$

Humedad absoluta

$$x_s = 0.622 \cdot \frac{p_{vs}}{p - p_{vs}}$$

$$x_s = f(t, p)$$



Grado de saturación

$$\varphi = \frac{x}{x_s}$$

$$\varphi = \frac{p_v}{p_{vs}} \cdot \frac{p - p_{vs}}{p - p_v} \quad \psi = \frac{p_v}{p_{vs}}$$

$$\varphi = \psi \cdot \frac{p - p_{vs}}{p - p_v}$$

$$\varphi \cong \psi$$

Ecuación de estado del aire húmedo

$$p_a \cdot v = R_a \cdot T$$

$$p_v \cdot v = x \cdot R_v \cdot T$$

$$(p_v + p_a) \cdot v = (R_a + x \cdot R_v) \cdot T$$

$$p = p_a + p_v$$

$$p \cdot v = (R_a + x \cdot R_v) \cdot T$$

$$R_a = 29.26 \cdot \frac{\text{kg} \cdot \text{m}}{\text{kg} \cdot \text{K}}$$

$$R_v = 47.07 \cdot \frac{\text{kg} \cdot \text{m}}{\text{kg} \cdot \text{K}}$$

Entalpía del aire húmedo no saturado

Aire seco, $h_0=0$ p/ $t_0=0^\circ\text{C}$

$$h_a = c_{pa} \cdot t \quad c_{pa} = 0.24 \frac{\text{kcal}}{\text{kg} \cdot ^\circ\text{C}}$$

Agua líquida, $h_0=0$ p/ $t_0=0^\circ\text{C}$

$$h_v = r_0 + c_{pv} \cdot t$$

$$c_{pv} = 0.46 \frac{\text{kcal}}{\text{kg} \cdot ^\circ\text{C}} \quad r_0 = 597 \frac{\text{kcal}}{\text{kg}}$$

1kg de aire seco + x kg de vapor de agua

$$h = 1h_a + x.h_v$$

$$h = c_{pa} \cdot t + x \cdot (r_0 + c_{pv} \cdot t) \quad \left[\frac{\text{kcal}}{\text{kg}(\text{as})} \right]$$

Entalpía del a.h. con niebla

1kg de aire seco + x_s kg de vapor + $(x - x_s)$ kg de agua líquida

$$h = h_a + x_s \cdot h_v + (x - x_s) \cdot h_1$$

$$h_1 = c_1 \cdot t$$

$$h = c_{pa} \cdot t + x_s \cdot (r_0 + c_{pv} \cdot t) + (x - x_s) \cdot c_1 \cdot t \quad \left[\frac{\text{kcal}}{\text{kg}(\text{as})} \right]$$

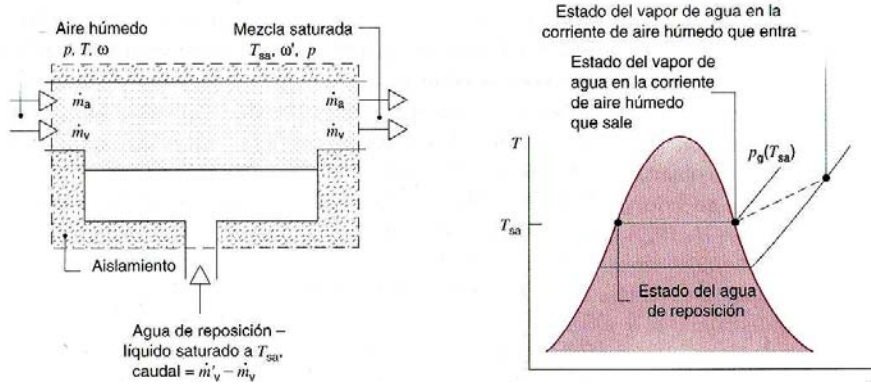
1kg de aire seco + x kg de vapor + $(x - x_s)$ kg de hielo

$$h = h_a + x_s \cdot h_v + (x - x_s) \cdot h_h$$

$$h_h = -f + c_{ph} \cdot t$$

$$h = c_{pa} \cdot t + x_s \cdot (r_0 + c_{pv} \cdot t) + (x - x_s) \cdot (-f + c_{ph} \cdot t)$$

Temperatura de saturación adiabática



$$h + (x_s - x) \cdot h_w = h_s \quad h \gg (x_s - x) \cdot h_w \quad h \cong h_s$$

$$c_{pa} \cdot t + x \cdot (r_o + c_{pv} \cdot t) + (x_s - x) \cdot c_{pw} \cdot t_s = c_{pa} \cdot t_s + x_s \cdot (r_o + c_{pv} \cdot t_s)$$

Temperatura de saturación adiabática

$$c_{pa} \cdot t + x \cdot (r_o + c_{pv} \cdot t) + (x_s - x) \cdot c_{pw} \cdot t_s = c_{pa} \cdot t_s + x_s \cdot (r_o + c_{pv} \cdot t_s)$$

$$c_{pa} \cdot t + x \cdot (r_o + c_{pv} \cdot t) + (x_s - x) \cdot c_{pw} \cdot t_s =$$

$$= c_{pa} \cdot t_s + (x_s - x) \cdot (r_o + c_{pv} \cdot t_s) + x \cdot (r_o + c_{pv} \cdot t_s)$$

$$(c_{pa} + x \cdot c_{pv}) \cdot t = (x_s - x) \cdot (r_o + c_{pv} \cdot t_s - c_{pw} \cdot t_s) + (c_{pa} + x \cdot c_{pv}) \cdot t_s$$

$$c_{pa} \gg x \cdot c_{pv} \quad r_o + c_{pv} \cdot t_s - c_{pw} \cdot t_s = h'' - h' = r$$

$$c_{pa} \cdot t = (x_s - x) \cdot r + c_{pa} \cdot t_s$$

$$t_s = t - \frac{(x_s - x) \cdot r}{c_{pa}}$$

Temperatura de saturación adiabática

$$h \cong h_s$$

$$c_{pa}.t + x.(r_o + c_{pv}.t) = c_{pa}.t_s + x_s.(r_o + c_{pv}.t_s)$$

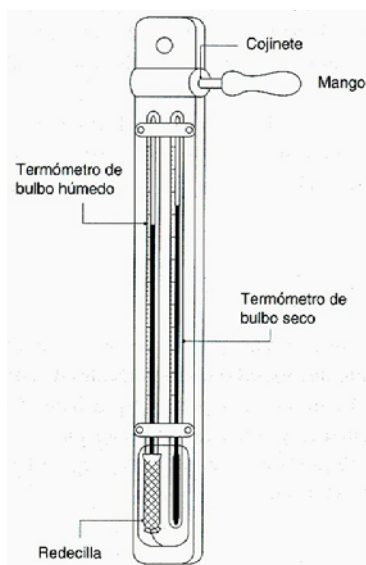
$$c_{pa}.t + x.r_o + x.c_{pv}.t = c_{pa}.t_s + x_s.r_o + x_s.c_{pv}.t_s$$

$$(c_{pa} + x.c_{pv}).t + x.r_o = (c_{pa} + x_s.c_{pv}).t_s + x_s.r_o$$

$$c_{pa}.t + (x - x_s).r_o = c_{pa}.t_s$$

$$t_s \cong t - \frac{(x_s - x).r_o}{c_{pa}}$$

Temperatura de bulbo húmedo



Cantidad de agua q se evapora

$$dw = \sigma.F.(x_s - x).d\tau$$

$$\delta Q_1 = r.dw$$

$$\delta Q_1 = r.\sigma.F.(x_s - x).d\tau$$

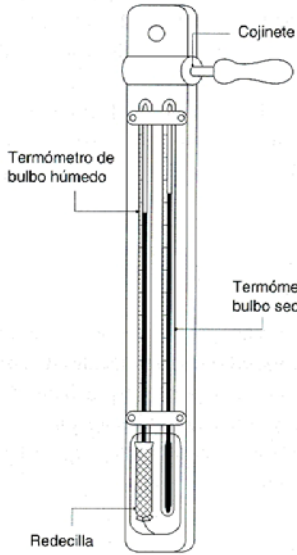
$$\delta Q_2 = k.F.(t_{bs} - t_{bh}).d\tau$$

$$r.\sigma.F.(x_s - x).d\tau = k.F.(t_{bs} - t_{bh}).d\tau$$

$$r.\sigma.(x_s - x) = k.(t_{bs} - t_{bh})$$

$$t_{bh} = t_{bs} - \frac{r.\sigma.(x_s - x)}{k}$$

Temperatura de bulbo húmedo



$$t_{bh} = t_{bs} - \frac{r \cdot \sigma \cdot (x_s - x)}{k}$$

$$t_s = t - \frac{(x_s - x) \cdot r}{c_{pa}}$$

$$\frac{r \cdot \sigma}{k} = \frac{r}{c_{pa}}$$

$$\frac{c_{pa} \cdot \sigma}{k} = 1 \quad \text{Relación de Lewis}$$

Diagrama psicrométrico

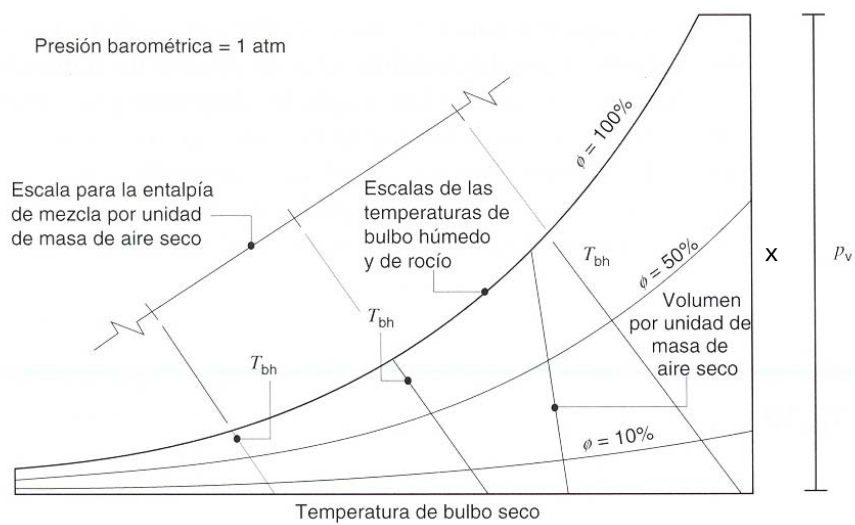
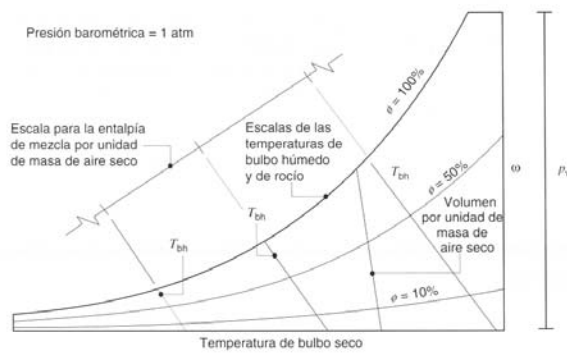


Diagrama psicrométrico



$$h = cp_a \cdot t + x \cdot r_0 + x \cdot cp_v \cdot t$$

$$dh = cp_a \cdot dt + r_0 \cdot dx + x \cdot cp_v \cdot dt + cp_v \cdot t \cdot dx = 0$$

$$(r_0 + cp_v \cdot t) dx = -(cp_a + x \cdot cp_v) dt$$

$$\left(\frac{\partial x}{\partial t}\right)_{h=cte} = -\frac{cp_a + x \cdot cp_v}{r_0 + cp_v \cdot t}$$

$$cp_a \gg x \cdot cp_v, r_0 \gg cp_v \cdot t$$

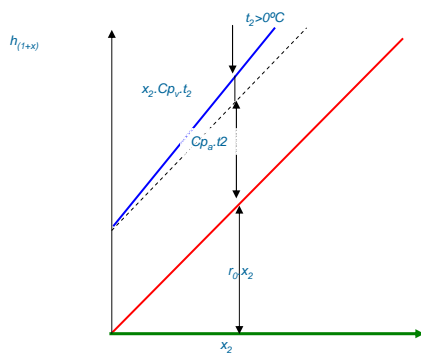
$$\left(\frac{\partial x}{\partial t}\right)_{h=cte} \cong -\frac{cp_a}{r_0}$$

$$p/x = 0 \Rightarrow h = cp_a \cdot t \Rightarrow t = \frac{h}{cp_a}$$

$$x_{s(t)} = 0.622 \cdot \frac{P_{vs(t)}}{p - P_{vs(t)}}$$

$$\varphi = \frac{x}{x_{s(t)}} \quad x_{(\varphi, t)} = x_{s(t)} \cdot \varphi$$

Diagrama entálpico



$p/t = cte \wedge$ aire no saturado

$$h = cp_a \cdot t + x \cdot (r_0 + cp_v \cdot t)$$

$$h = r_0 \cdot x + cp_a \cdot t + x \cdot cp_v \cdot t$$

$$\left(\frac{\partial h}{\partial x}\right)_t = r_0 + cp_v \cdot t$$

$p/t = 0^\circ C \wedge$ aire no saturado

$$h = r_0 \cdot x$$

$$\left(\frac{\partial h}{\partial x}\right)_t = r_0$$

Diagrama entálpico

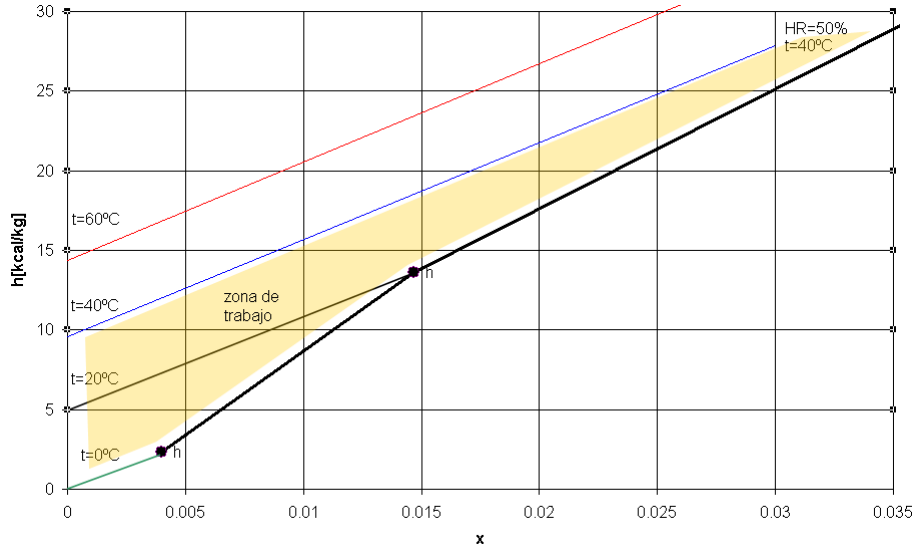
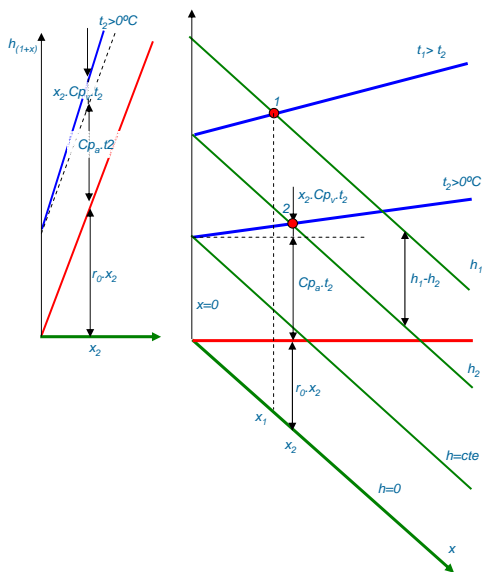


Diagrama entálpico



$p/t = cte \wedge$ aire no saturado

$$h = cp_a \cdot t + x \cdot (r_0 + cp_v \cdot t)$$

$$h = r_0 \cdot x + cp_a \cdot t + x \cdot cp_v \cdot t$$

$$\left(\frac{\partial h}{\partial x}\right)_t = r_0 + cp_v \cdot t$$

$p/t = 0^\circ C \wedge$ aire no saturado

$$h = r_0 \cdot x$$

$$\left(\frac{\partial h}{\partial x}\right)_t = r_0$$

Diagrama entálpico

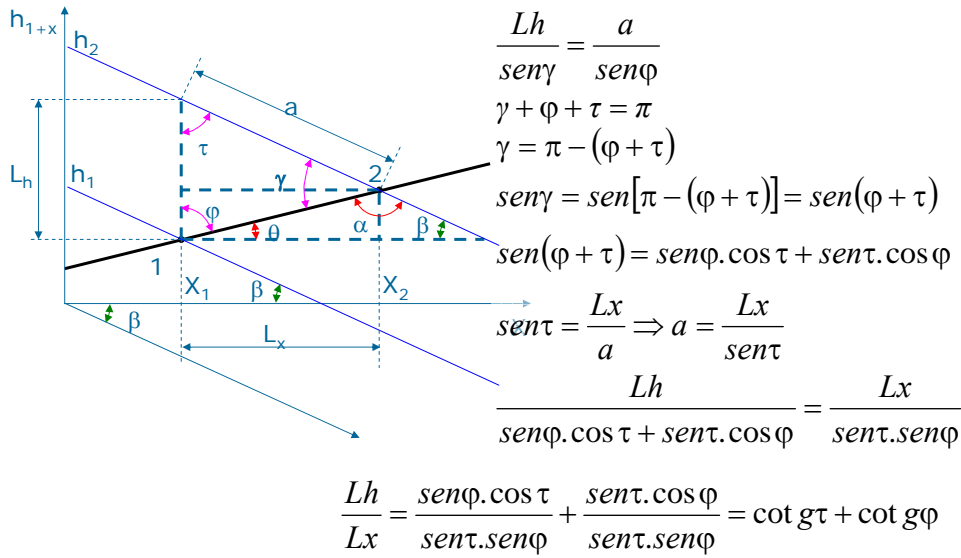


Diagrama entálpico

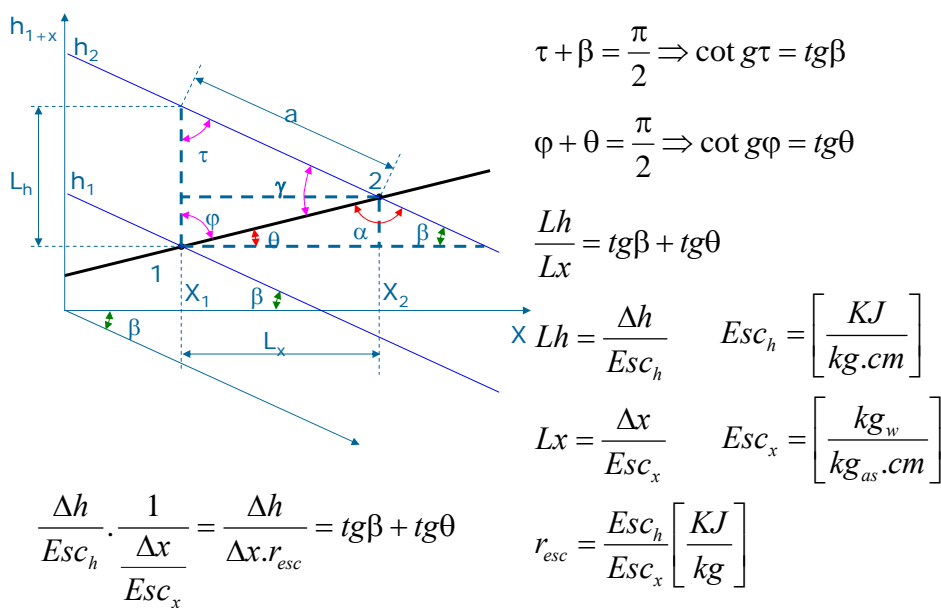
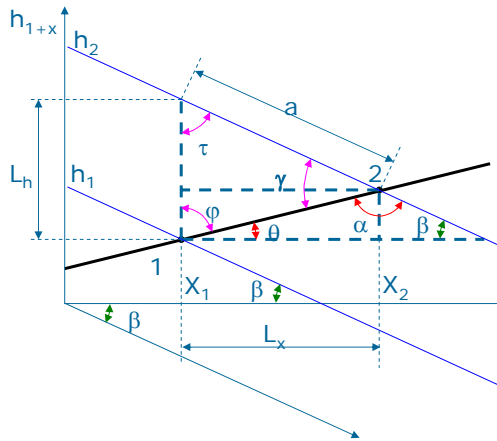


Diagrama entálpico



$$\frac{\Delta h}{\Delta x \cdot r_{esc}} = tg\beta + tg\theta$$

$$p/h = cte \Rightarrow \Delta h = 0 \Rightarrow tg\theta = -tg\beta \Rightarrow \theta = -\beta$$

$$p/x = cte \Rightarrow \Delta x = 0 \Rightarrow tg\beta + tg\theta = \infty \Rightarrow \theta = \frac{\pi}{2}$$

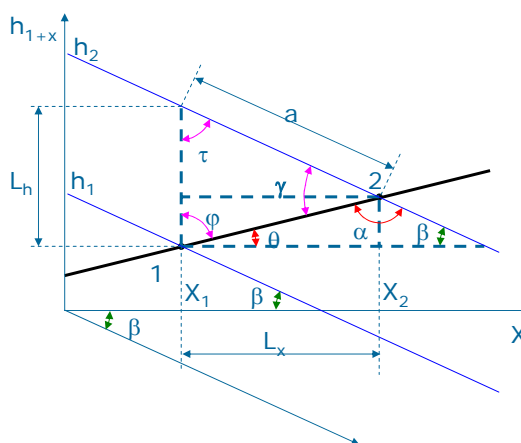
$p/t = cte \wedge$ aire no saturado

$$h = cp_a \cdot t + x \cdot (r_0 + cp_v \cdot t)$$

$$\left(\frac{\partial h}{\partial x}\right)_t = r_0 + cp_v \cdot t$$

$$p/t = 0^\circ C \quad \left(\frac{\partial h}{\partial x}\right)_t = r_0$$

Diagrama entálpico



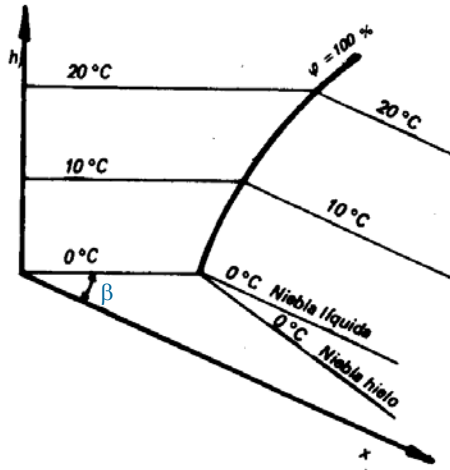
$$\frac{\Delta h}{\Delta x \cdot r_{esc}} = tg\beta + tg\theta$$

$$\frac{r_0}{r_{esc}} = tg\beta + tg\theta$$

Adopto $\theta = 0$ $p/t = 0^\circ C$

$$tg\beta = \frac{r_0}{r_{esc}}$$

Diagrama entálpico



$p/t = cte \wedge$ niebla líquida

$$h = cp_a \cdot t + x_s(r_0 + cp_v \cdot t) + (x - x_s) \cdot c_l \cdot t$$

$$\left(\frac{\partial h}{\partial x}\right)_t = c_l \cdot t$$

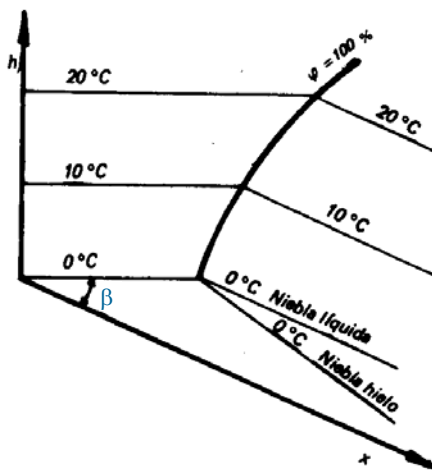
$$\frac{c_l \cdot t}{r_{esc}} = tg\beta + tg\theta = \frac{r_0}{r_{esc}} + tg\theta$$

$$tg\theta = \frac{-r_0}{r_{esc}} + \frac{c_l \cdot t}{r_{esc}}$$

$p/t = 0^\circ C \wedge$ niebla líquida

$$tg\theta = \frac{-r_0}{r_{esc}} = -tg\beta \quad \theta = -\beta$$

Diagrama entálpico



$p/t = cte \wedge$ niebla hielo

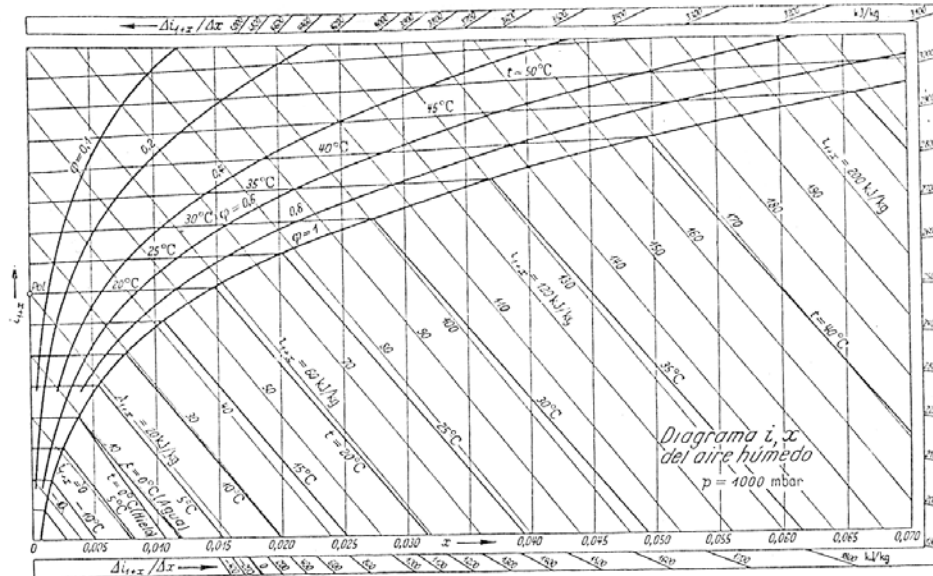
$$h = cp_a \cdot t + x \cdot (r_0 + cp_v \cdot t) + (x - x_s) \cdot (-f + cp_h \cdot t)$$

$$\left(\frac{\partial h}{\partial x}\right)_t = -f + cp_h \cdot t$$

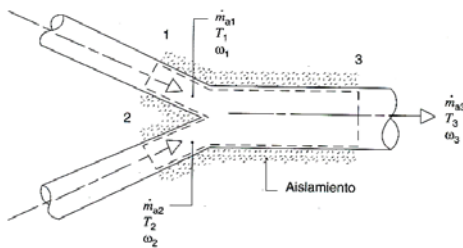
$$\frac{-f + cp_h \cdot t}{r_{esc}} = tg\beta + tg\theta = \frac{r_0}{r_{esc}} + tg\theta$$

$$tg\theta = \frac{-r_0}{r_{esc}} + \frac{-f}{r_{esc}}$$

Diagrama entálpico



Mezcla de corrientes de a.h.



Conservación de la materia

$$m = m_1 + m_2$$

$$m \cdot x = m_1 \cdot x_1 + m_2 \cdot x_2$$

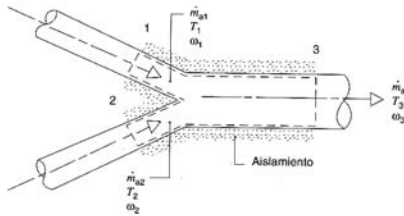
$$x = \frac{m_1 \cdot x_1 + m_2 \cdot x_2}{m_1 + m_2}$$

Conservación de la energía (PP)

$$m \cdot h = m_1 \cdot h_1 + m_2 \cdot h_2$$

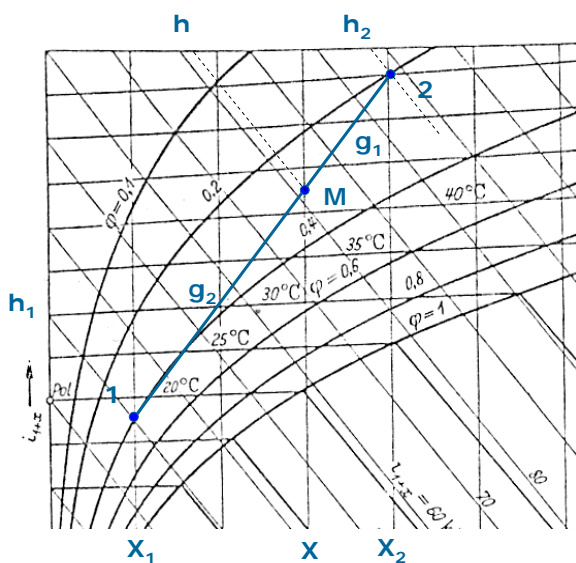
$$h = \frac{m_1 \cdot h_1 + m_2 \cdot h_2}{m_1 + m_2}$$

Mezcla de corrientes de a.h.



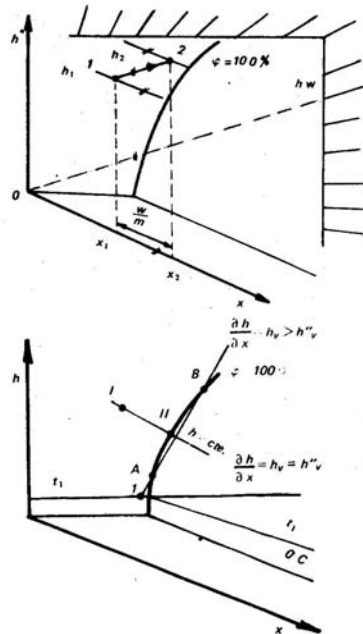
$$\begin{aligned}
 m_1 \cdot x + m_2 \cdot x &= m_1 \cdot x_1 + m_2 \cdot x_2 \\
 m_2 \cdot x - m_2 \cdot x_2 &= m_1 \cdot x_1 - m_1 \cdot x \\
 m_2 \cdot (x - x_2) &= m_1 \cdot (x_1 - x) \\
 m_1 \cdot h + m_2 \cdot h &= m_1 \cdot h_1 + m_2 \cdot h_2 \\
 m_2 \cdot h - m_2 \cdot h_2 &= m_1 \cdot h_1 - m_1 \cdot h \\
 m_2 \cdot (h - h_2) &= m_1 \cdot (h_1 - h) \\
 \frac{m_2 \cdot (h - h_2)}{m_2 \cdot (x - x_2)} &= \frac{m_1 \cdot (h_1 - h)}{m_1 \cdot (x_1 - x)} \\
 \frac{h_2 - h}{x_2 - x} &= \frac{h - h_1}{x - x_1}
 \end{aligned}$$

Mezcla de corrientes de a.h.



$$\begin{aligned}
 x &= \frac{m_1 \cdot x_1 + m_2 \cdot x_2}{m_1 + m_2} \\
 g_1 &= \frac{m_1}{m} \wedge g_2 = \frac{m_2}{m} \\
 x &= g_1 \cdot x_1 + g_2 \cdot x_2 \\
 g_1 + g_2 &= 1 \\
 x &= (1 - g_2) \cdot x_1 + g_2 \cdot x_2 \\
 x &= x_1 - g_2 \cdot x_1 + g_2 \cdot x_2 \\
 g_2 &= \frac{x - x_1}{x_2 - x_1} = \frac{\overline{1M}}{\overline{1_2}} \\
 \overline{1M} &= \overline{1_2} \cdot g_2
 \end{aligned}$$

Humidificación



Incorporación de agua en estado líquido o de vapor a una corriente de aire húmedo

$$m \cdot x_1 + W = m \cdot x_2$$

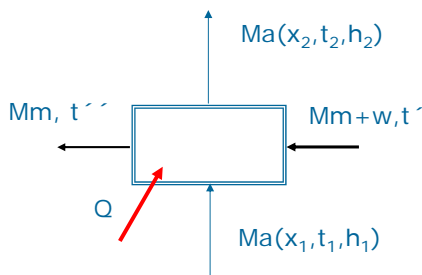
$$x_2 - x_1 = \frac{W}{m}$$

$$m \cdot h_1 + W \cdot h_w = m \cdot h_2$$

$$h_2 - h_1 = \frac{W}{m} h_w$$

$$\frac{h_2 - h_1}{x_2 - x_1} = h_w$$

Secado



Material no higroscópico

$$m_a \cdot x_1 + W = m_a \cdot x_2$$

$$W = m_a \cdot (x_2 - x_1)$$

$$m_a \cdot h_1 + m_m \cdot h_{m1} + W \cdot h_w + Q = m_a \cdot h_2 + m_m \cdot h_{m2}$$

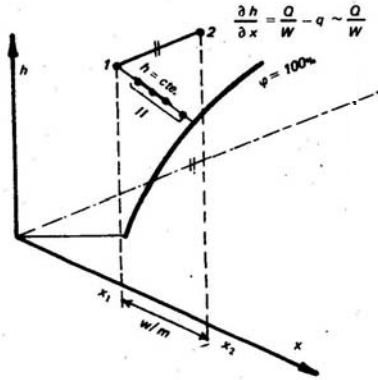
$$Q = m_a \cdot (h_2 - h_1) + m_m \cdot (h_{m2} - h_{m1}) - W \cdot h_w$$

$$h_{m2} - h_{m1} = c_m (t'' - t')$$

$$h_w = c_w \cdot t'$$

$$Q = m_a \cdot (h_2 - h_1) + m_m \cdot c_m (t'' - t') - W \cdot c_w \cdot t'$$

Secado



$$Q = m_a \cdot (h_2 - h_1) + m_m \cdot c_m (t'' - t') - W \cdot c_w \cdot t'$$

$$W = m_a \cdot (x_2 - x_1)$$

$$\frac{Q}{W} = \frac{h_2 - h_1}{x_2 - x_1} + \frac{m_m \cdot c_m}{W} (t'' - t') - c_w \cdot t'$$

Llamando q a:

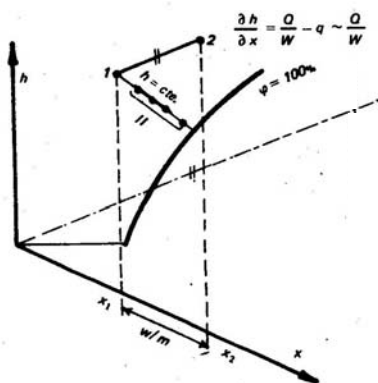
$$q = \frac{m_m \cdot c_m}{W} (t'' - t') - c_w \cdot t'$$

$$\frac{Q}{W} = \frac{h_2 - h_1}{x_2 - x_1} + q$$

Despreciando el valor de q

$$\frac{Q}{W} = \frac{h_2 - h_1}{x_2 - x_1}$$

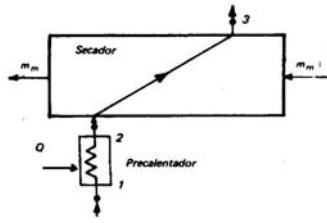
Secado



$$x_2 = x_1 + \frac{W}{m_a}$$

$$\frac{h_2 - h_1}{x_2 - x_1} = \frac{Q}{W} - q \cong \frac{Q}{W}$$

Secado con precalentador



$$m_a = \frac{W}{x_3 - x_2} = \frac{W}{x_3 - x_1}$$

$$Q = m_a(h_2 - h_1) = m_a(h_3 - h_1)$$

$$\frac{Q}{W} = \frac{h_3 - h_1}{x_3 - x_1}$$

